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Reg. No.	:	
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Name :



Third Semester B.Sc. Degree Examination, March 2022

First Degree Programme Under CBCSS

Mathematics

Complementary Course for Chemistry and Polymer Chemistry

MM 1331.2 : MATHEMATICS III – LINEAR ALGEBRA, PROBABILITY THEORY AND NUMERICAL METHODS

(2019 & 2020 Admission)

Time: 3 Hours Max. Marks: 80

SECTION - I

All the first 10 questions are compulsory. Each carries 1 mark.

- 1. Define the transpose of a matrix.
- 2. Evaluate the determinant $\begin{vmatrix} 0 & 3 & -2 \\ -3 & 7 & -4 \\ 0 & 6 & 0 \end{vmatrix}$.
- 3. Write a symmetric equation of a straight line.
- 4. Define Kronecker δ .
- 5. What is the cross product of two vectors?
- 6. Give a definition of the concept 'Probability of an event E'.

- 7. There are 10 questions and you are to do 8 of them. In how many ways can you choose them?
- 8. Write Baye's formula for conditional probability.
- 9. Write the expression for variance of a random variable x and explain the terms.
- 10. What is a transcendental equation?

 $(10 \times 1 = 10 \text{ Marks})$

SECTION - II

Answer any eight questions. Each carries 2 marks.

- 11. Evaluate the determinant | 1 -5 2 | 7 3 4 | 2 1 5 |
- 12. Find a vector perpendicular to both the vectors A = 2i + j k and B = i + 3j 2k.
- 13. Find the rank of the matrix $\begin{pmatrix} 2 & -3 & 5 & 3 \\ 4 & -1 & 1 & 1 \\ 3 & -2 & 3 & 4 \end{pmatrix}$.
- 14. Find the parametric equation of the line through (1, -1, -5) and (2, -3, -3).
- 15. Define linear operator.
- 16. Is square root a linear operator? Why?
- 17. A three digit number is selected at random. What is the probability that all three digits are the same?
- 18. Two dice are rolled. What is the probability that the sum is ≥ 10?

- 19. Define mutually exclusive events.
- 20. If P(A) = 0.07755, P(AB) = 0.038, find $P_A(B)$.
- 21. A card is selected from a shuffled deck. What is the probability that it is either a king or a club? That it is both a king and a club?
- 22. A club consists of 50 members. In how many ways can a president, vice president, secretary and treasurer be chosen?
- 23. Write an iteration scheme for finding the square root of X.
- 24. What is binary chopping?
- 25. Evaluate the integral $I = \int_{0}^{1} \frac{1}{1+x^2} dx$ using the Simpson's rule.
- 26. Write Newton-Raphson iteration formula.

$$(8 \times 2 = 16 \text{ Marks})$$

Answer any six questions. Each carries 4 marks.

27. Evaluate the determinant
$$D = \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$
.

28. Write and row reduce the augmented matrix for the equations :

$$x-y+4z = 5$$

 $2x-3y+8z = 4$
 $x-2y+4z = 9$.

29. Using Cramer's rule solve the set of equations :

$$2x + 3y = 3$$

$$x-2y=5$$

- 30. Find the equation of a line through (1, 0, -2) and perpendicular to the plane 3x-4y+z+6=0.
- 31. Find the distance between the lines r = i 2j + (i k)t and r = 2j k + (j i)t.
- 32. Which is the most probable sum in a toss of two dice? What is its probability?
- 33. Two students are working separately on the same problem. If the first student has probability $\frac{1}{2}$ of solving it and the second student has probability $\frac{3}{4}$ of solving it, what is the probability that atleast one of them solves it?
- 34. Find the coefficient of x^8 in the binomial expansion of $(1+x)^{15}$.
- 35. Using Baye's formula find the probability of all heads in three tosses of a coin if you know that atleast one is a head?
- 36. Find an explicit formula that will generate a random number y distributed on $(-\infty, \infty)$ according to the Cauchy distribution $f(y)dy = \left(\frac{a}{\pi}\right)\frac{dy}{a^2+y^2}$, given a random number ξ uniformly distributed on (0, 1).
- 37. Evaluate $I = \int_{0}^{2} (x^2 3x + 4) dx$ using trapezium rule with h = 0.5.
- 38. Find the numerical solution of the equation $\frac{dy}{dx} = 2y^{\frac{3}{2}}$, y(0) = 1, for x = 0.1 to 0.5 in steps of 0.1.

 $(6 \times 4 = 24 \text{ Marks})$

SECTION - IV

Answer any two questions. Each carries 15 marks.

- 39. Find the rotation matrix C if the quadratic surface $x^2 + 6xy 2y^2 2yz + z^2 = 24$ is rotated to principal axis.
- 40. Find the eigen values and eigen vectors of the matrix $M = \begin{pmatrix} 1 & -4 & 2 \\ -4 & 1 & -2 \\ 2 & -2 & -2 \end{pmatrix}$.
- 41. If two dice are rolled:
 - (a) What is the probability that the sum of the numbers on the dice will be 5? (3)
 - (b) What is the probability that the sum on the dice is divisible by 5? (3)
 - (c) What is the most probable sum in a toss of two dice? What is its probability?
 - (d) What is the probability that the sum on the dice is greater than or equal to 9?
 (3)
 - (e) If the sum is odd, what is the probability that it is equal to 7? (3)
- 42. Derive the Poison density function $P_n = \frac{\mu^n}{n!} e^{-\mu}$.
- 43. Explain:
 - (a) Stratified sampling method. (5)
 - (b) Control variates method. (5)
 - (c) Hit or miss method. (5)

44. Solve the simultaneous equations :

$$x_1 + 6x_2 - 4x_3 = 8$$
$$3x_1 - 20x_2 + x_3 = 12$$
$$-x_1 + 3x_2 + 5x_3 = 3$$

using Gaussian elimination.

 $(2 \times 15 = 30 \text{ Marks})$